

Algebra II

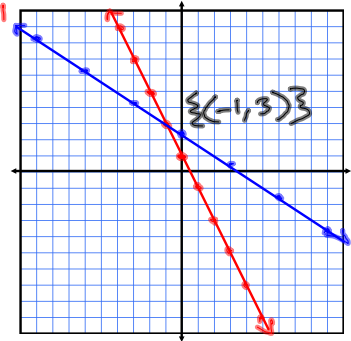
SS-1

Systems of Linear Equations in Two Variables

Solving Systems - The Graphing Method (pg 218)

$$1) \begin{cases} 2x + y = 1 \\ 2x + 3y = 7 \end{cases} \quad \begin{aligned} y &= -2x + 1 \\ m &= -2 \\ b &= 1 \end{aligned}$$

$$\begin{aligned} \frac{3y}{3} &= \frac{-2x+7}{3} \\ y &= -\frac{2}{3}x + \frac{7}{3} \\ m &= -\frac{2}{3} \quad b = \frac{7}{3} \end{aligned}$$



Solving Systems - The Substitution Method

$$1) \begin{cases} 2x + y = 1 \\ 2x + 3y = 7 \end{cases} \rightarrow y = -2x + 1$$

$$-2(-1) + 1 = y$$

$$2 + 1 = y$$

$$3 = y$$

$$2x + 3(-2x + 1) = 7$$

$$2x - 6x + 3 = 7$$

$$-4x = 4$$

$$x = -1$$

$$\{(-1, 3)\}$$

Solving Systems - The Linear Transformation Method

$$1) \begin{cases} 2x + y = 1 \\ 2x + 3y = 7 \end{cases} \begin{aligned} (-1) &\rightarrow -2x - y = -1 \\ + & 2x + 3y = 7 \\ \hline & 2y = 6 \\ & y = 3 \end{aligned}$$

$$2x + (3) = 1$$

$$2x = -2$$

$$x = -1$$

$$\{(-1, 3)\}$$

Methods for Solving Systems

	Pros	Cons
Graphing	Easy if both are in $y = mx + b$ form	Long, might cross off the graph, inaccurate
Substitution	Use when it's easy to get a variable alone.	Can turn into ugly fractions fast!
Linear Transformation	usually easiest and fastest	Comparitively none.

$$13) \begin{cases} y = -x + 3 \\ y = x - 4 \end{cases}$$

$$+ \begin{aligned} y &= -x + 3 \\ y &= x - 4 \\ \hline 2y &= -1 \\ y &= -\frac{1}{2} \end{aligned}$$

$$\left(-\frac{1}{2}\right) = x - 4$$

$$3\frac{1}{2} = x$$

$$\left\{\left(\frac{7}{2}, -\frac{1}{2}\right)\right\}$$

17) $\begin{cases} 3x + 3y = 6 \\ 5x - 6y = 15 \end{cases}$ 2

$\begin{cases} 6x + 6y = 12 \\ 5x - 6y = 15 \end{cases}$

$\frac{11x}{11} = \frac{27}{11}$

$x = \frac{27}{11}$

$\left\{ \left(\frac{27}{11}, -\frac{5}{11} \right) \right\}$

$x + y = 2$

$\frac{27}{11} + y = 2$

$y = 2 - \frac{27}{11}$

$y = \frac{22}{11} - \frac{27}{11}$

$= -\frac{5}{11}$

29) $\begin{cases} 3x = 4y - 4 \\ 4y = 3x - 3 \end{cases}$

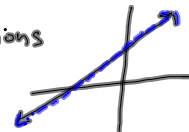
$3x = (3x - 3) - 4$

$3x = 3x - 7$

$0 = -7$

\emptyset

$0 = 0$
infinite solutions



33) $\left(\frac{6}{u} + \frac{3}{v} = 2 \right)$ 3

$\frac{2}{u} - \frac{9}{v} = 4$

$\frac{18}{u} + \frac{9}{v} = 6$

$\frac{2}{u} - \frac{9}{v} = 4$

$\frac{20}{u} = 10$

$u = 2$

$\frac{2}{2} - \frac{9}{v} = 4$

$1 - \frac{9}{v} = 4$

$-\frac{9}{v} = 3$

$\frac{9}{v} = -3$

$v = -3$

$\left\{ (2, -3) \right\}$

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